

GCE Examinations  
Advanced Subsidiary / Advanced Level  
**Statistics**  
**Module S3**

Paper B

## **MARKING GUIDE**

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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### S3 Paper B – Marking Guide

1. (a) divide population into distinct groups  
sample sizes from each group determined by proportions in population  
sample any member of group until quota is filled B3
- (b) e.g. non-random sample within strata so may be biased B1
- (c) e.g. survey on political attitudes according to age group  
too time-consuming / impractical to random sample within strata B2 (6)
- 
2. exp. freq.  $0-45 = \frac{45}{360} \times 96 = 12$  etc. giving exp. freqs. 12, 12, 24, 24, 12, 12 M1 A1  
 $H_0$  : continuous uniform distribution is a suitable model  
 $H_1$  : continuous uniform distribution is not a suitable model B1
- | $O$ | $E$ | $(O - E)$ | $\frac{(O-E)^2}{E}$ |
|-----|-----|-----------|---------------------|
| 18  | 12  | 6         | 3                   |
| 19  | 12  | 7         | 4.0833              |
| 15  | 24  | -9        | 3.375               |
| 20  | 24  | -4        | 0.6667              |
| 9   | 12  | -3        | 0.75                |
| 15  | 12  | 3         | 0.75                |
- $\therefore \sum \frac{(O-E)^2}{E} = 12.625$  M1 A2  
 $v = 6 - 1 = 5, \chi^2_{\text{crit}}(5\%) = 11.070$  M1 A1  
 $12.625 > 11.070 \therefore$  reject  $H_0$   
 continuous uniform distribution is not a suitable model A1 (9)
- 
3. (a) mean =  $\frac{(46 \times 60) + 15}{20} = 138.75$  M1  
 C.I.  $\bar{x} \pm 1.6449 \frac{\sigma}{\sqrt{n}} = 138.75 \pm 1.6449 \cdot \frac{23}{\sqrt{20}}$  M1 A1  
 giving (130.3, 147.2) A2
- (b) width =  $2 \times 1.6449 \times \frac{23}{\sqrt{n}} \therefore 2 \times 1.6449 \times \frac{23}{\sqrt{n}} < 10$  M1 A1  
 $\therefore \sqrt{n} > 7.56654$  A1  
 giving  $n > 57.25$  so min. value of  $n = 58$  M1 A1
- (c) e.g. she might buy big-budget movies with longer credits B1 (11)
- 
4. expected freq. 8am-6pm/minor =  $\frac{108 \times 56}{148} = 40.86$   
 6pm-2am/minor =  $\frac{108 \times 71}{148} = 51.81$  M1 A2  
 giving expected freqs
- |       |       |
|-------|-------|
| 40.86 | 15.14 |
| 51.81 | 19.19 |
| 15.33 | 5.67  |
- $H_0$  : proportion of serious injuries independent of time  
 $H_1$  : proportion of serious injuries varies with time B1
- | $O$ | $E$   | $(O - E)$ | $\frac{(O-E)^2}{E}$ |
|-----|-------|-----------|---------------------|
| 45  | 40.86 | 4.14      | 0.4195              |
| 11  | 15.14 | -4.14     | 1.1321              |
| 49  | 51.81 | -2.81     | 0.1524              |
| 22  | 19.19 | 2.81      | 0.4115              |
| 14  | 15.33 | -1.33     | 0.1154              |
| 7   | 5.67  | 1.33      | 0.3120              |
- $\therefore \sum \frac{(O-E)^2}{E} = 2.543$  M1 A2  
 $v = 2, \chi^2_{\text{crit}}(5\%) = 5.991$  M1 A1  
 $2.543 < 5.991 \therefore$  not significant  
 there is no evidence of prop'n of serious injuries varying with time A1 (11)

5.	(a)	<table border="0"> <thead> <tr> <th>bottle</th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> <th>F</th> <th>G</th> <th>H</th> <th>I</th> <th>J</th> </tr> </thead> <tbody> <tr> <td>enth. rank</td> <td>4</td> <td>7</td> <td>2</td> <td>1</td> <td>8</td> <td>6</td> <td>5</td> <td>10</td> <td>9</td> <td>3</td> </tr> <tr> <td>price rank</td> <td>1</td> <td>6</td> <td>2</td> <td>3</td> <td>10</td> <td>7</td> <td>9</td> <td>4</td> <td>8</td> <td>5</td> </tr> <tr> <td><math>d^2</math></td> <td>9</td> <td>1</td> <td>0</td> <td>4</td> <td>4</td> <td>1</td> <td>16</td> <td>36</td> <td>1</td> <td>4</td> </tr> </tbody> </table>	bottle	A	B	C	D	E	F	G	H	I	J	enth. rank	4	7	2	1	8	6	5	10	9	3	price rank	1	6	2	3	10	7	9	4	8	5	$d^2$	9	1	0	4	4	1	16	36	1	4	
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$d^2$	9	1	0	4	4	1	16	36	1	4																																					
		$\Sigma d^2 = 76$		M2 A2																																											
		$r_s = 1 - \frac{6 \times 76}{10 \times 99} = 0.5394$		M1 A1																																											
	(b)	$H_0 : \rho = 0 \quad H_1 : \rho > 0$ $n = 10, 5\% \text{ level} \therefore \text{C.R. is } r_s > 0.5636$ $0.5394 < 0.5636 \therefore \text{not significant}$ there is no evidence of positive correlation		B1 M1 A1 A1																																											
	(c)	share ranks, both 6.5, use pmcc		B2 (12)																																											
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6.	(a)	$\hat{\mu} = \bar{V} = \frac{10367}{80} = 129.6 \text{ cm}$ $\hat{\sigma}^2 = s^2 = \frac{80}{79} \left( \frac{1350314}{80} - 129.5875^2 \right) = 87.09$		M1 A1 M2 A1																																											
	(b)	$H_0 : \mu_V = \mu_M \quad H_1 : \mu_V \neq \mu_M$ 1% level $\therefore \text{C.R. is } z < -2.5758 \text{ or } z > 2.5758$ test statistic = $\frac{129.6 - 130.5}{\sqrt{\frac{87.09}{80} + \frac{96.24}{280}}} = -0.7520$ not in C.R. do not reject $H_0$ no evidence of difference in mean heights		B1 B1 M2 A2 M1 A1 (13)																																											
<hr/>																																															
7.	(a)	let $X = \text{time to mark P1 paper}$ let $A = X_1 - X_2 \therefore A \sim N(0, 2 \times 17^2) = \sim N(0, 578)$ $P(-5 < A < 5) = P\left(\frac{-5-0}{\sqrt{578}} < Z < \frac{5-0}{\sqrt{578}}\right)$ $= P(-0.21 < Z < 0.21) = 0.5832 - (1 - 0.5832) = 0.166$		M1 A1 M1 A1 M1 A1																																											
	(b)	let $M = \text{time to mark M1 paper}$ , let $S = \text{time to mark S1 paper}$ let $T = M_1 + \dots + M_{45} + S_1 + \dots + S_{80}$ $\therefore T \sim N(45 \times 314 + 80 \times 284, 45 \times 42^2 + 80 \times 29^2) = \sim N(36\,850, 146\,660)$ $P(\text{time} < 10 \text{ hours}) = P(T < 36\,000) = P\left(Z < \frac{36\,000 - 36\,850}{\sqrt{146\,660}}\right)$ $= P(Z < -2.22) = 1 - 0.9868 = 0.0132$		M2 A2 M1 M1 A1 (13)																																											
				Total (75)																																											

